## IAPM:

## Illustration 1

Calculate the expected rate of return from the following information relating to B Ltd.

| State of the Economy <br> Boom | Probability of Occurrence <br> 0.30 | Rate of Return <br> $40 \%$ |
| :--- | :--- | :--- |
| Normal | 0.50 | $30 \%$ |
| Recession | 0.20 | $20 \%$ |

## Illustration 2

An investor would like to find the expected return on the share of Golden Ltd. The following data have been available:

State of the Economy Probability of Occurrence Rate of Return (\%)
Boom

| Normal | 0.30 | 30 |
| :--- | :--- | :--- |
| Recession | 0.50 | 18 |
|  | 0.20 | 10 |

Calculate the expected return from the share.

## Illustration 3

Given below are the likely returns in case of shares of VCC Ltd. and LCC Ltd. in the various economic conditions. Both the shares are presently quoted at 100 per share.

| Economic <br> Conditions | Probability | Returns of <br> VCC Ltd. | Returns of <br> LCC Ltd. |
| :--- | :--- | :--- | :--- |
| High Growth | 0.3 | 100 | 150 |
| Low Growth | 0.4 | 110 | 130 |
| Stagnation | 0.2 | 120 | 90 |
| Recession | 0.1 | 140 | 60 |

Which of the two companies are risky investments?

## Illustration 4

The rate of return of stocks of A and B under different states of economy are presented below along with the probability of the occurrence of each state of the economy.

Boom Normal Recession

| Probability of Occurrence |  |  |  |
| :--- | ---: | ---: | ---: |
| Rate of Return on stock A (\%) | 0.3 | 0.4 | 0.3 |
| Rate of Return on stock B (\%) | 20.0 | 30.0 | 50.0 |
|  | 50.0 | 30.0 | 20.0 |

(a) Calculate the expected rate of return and standard deviation of return for stocks A and for stocks B.
(b) If you could invest in either stocks A or stocks B, but not in both, which stock would you prefer and why?
(c) If the rate of return on stocks A was revised as shown below, would your preference in question (b) above change? Why?

|  | Boom | Normal | Recession |
| :--- | :--- | :--- | :--- |
| Rate of Return on stock A (\%) | 50.0 | 40.0 | 30.0 |

## Illustration 5

Shankar has been considering investment in stock X or Y . He has estimated the following distribution of returns of stock X and Stock Y.

| Return on stock X | Return on stock Y | Probability |
| :--- | :--- | :--- |
| 10 | 05 | 10 |
| 0 | 10 | 25 |
| 10 | 15 | 40 |
| 20 | 20 | 20 |
| 30 | 25 | 05 |

## Illustration 6

The rate of return on Stocks X and Y under different states of the economy are given below:

## Boom Normal Recession

| Probability of occurrence | 0.35 | 0.50 | 0.15 | (i) Calculate the <br> expected return and |
| :--- | ---: | ---: | :---: | :--- |
| Rate of Return on stock X (\%) <br> Rate of Return on stock Y (\%) | 20 | 30 | 40 | standard deviation of <br> return on both the <br> stocks. |
|  | 40 | 30 | 20 | (ii) If you could invest |

in either stocks X or stock Y , but not in both, which stock would you prefer?
(iii) What would be your decision if the probability changes to $0.30: 0.40: 0.30$ ?

## Illustration 7

Calculate the holding period return in the following example:
A Ltd. ()
B Ltd. ()

Price as on 31-3-2017
$20 \quad 10$
Price as on 31-3-2018
Dividend for the year 15
15
$1 \quad 1$

## Illustration 8

In January 2011, Mr. Dhimant Kapadia purchased the following 5 scrips:

| Co.'s Name | No. of Shares | Purchase Price |
| :--- | :--- | :--- |
| H Ltd. | 100 | 250 |
| C Ltd. | 100 | 180 |
| S Ltd. | 100 | 80 |
| F Ltd. | 100 | 240 |
| M Ltd. | 100 | 260 |

He paid brokerage of 1,500
During the year 2011, Mr. Dhimant Kapadia received the following:

| Co's Name | Dividend | Bonus Shares |
| :--- | :--- | :--- |
| H Ltd. | 300 | $1: 2$ |
| C Ltd. | 290 |  |
| S Ltd. | 450 |  |
| F Ltd. | 500 |  |
| M Ltd. | 600 |  |

In January 2018, Mr. D sold all his holdings at the following prices:

| Co's Name | Market Price |
| :--- | :--- |
| H Ltd. | 275 |

C Ltd. 240
S Ltd.
108
F Ltd.

M Ltd.
400

He paid brokerage of 1,865 .
Calculate the holding period return.
Illustration 9
Dr. Shah purchased 400 shares of Sundar Ltd. @ 61 each on $15^{\text {th }}$ Oct 2008. He paid a brokerage of 600 . The company paid the following dividends:

| June 2009 | 800 |
| :--- | :--- |
| June 2010 | 1000 |
| June 2011 | 1,200 |

He sold his holdings for 34,500 (net) on 15th October, 2011.
(1) What is the holding period return? (2) What is the annualized return? (3) Is Mr. Shah a good investor?

## Illustration 10

Mr. Ashok purchased 10 shares of ACC Ltd. four years ago at 50 each. The company paid the following dividends.

## Year 1 Year 2 Year 3 Year 4

| Dividend per Share <br> Dividend Amount () | 2 | 2 | 2.5 | 3 |
| :--- | :--- | :--- | :--- | :--- |
|  | 20 | 20 | 25 | 30 |

The current price of the share is 60 . What rate of return has he earned on his investment if he sells the shares now?

## Illustration 11

You own a portfolio that is $60 \%$ invested in Stock X, $25 \%$ in stock Y and balance in Stock Z. The excepted returns on these stocks are $12 \%, 16 \%$ and $19 \%$ respectively. What is the expected return on the portfolio?

Illustration 12
You have 10000 to invest in a stock portfolio. Your choices are Stock X with an expected return of $18 \%$ and Stock Y with an expected return of $11 \%$. If your goal is to create a portfolio with an excepted return of $16.5 \%$, how much money will you invest in Stock X and in Stock Y ?

Illustration 13
Rahul invest the following sums of money in common stocks having expected return as follows:

| Security | Amount Invested () | Expected Return |
| :--- | :--- | :--- |
| Moser Baer | 6000 | $14 \%$ |
| Kirloskar Cummins | 11000 | $16 \%$ |
| FDC Ltd. | 9000 | $17 \%$ |
| Novartis India | 7000 | $13 \%$ |


| GTL | 5000 | $20 \%$ |
| :--- | :--- | :--- |
| Pfizer | 13000 | $15 \%$ |
| Excel Industry | 9000 | $18 \%$ |

1. What is the expected $\%$ return on his portfolio?
2. What would be his expected return if Rahul quadruples his investment in GTL while leaving everything else the same?

## Illustration 14

The common stocks of Bajaj and TVS have expected returns of $15 \%$ and $20 \%$ respectively, while the standard deviations are $20 \%$ and $40 \%$. The excepted correlation coefficient between the two stocks is 0.36 . What is the excepted value of return and the standard deviation of a portfolio consisting of: (a) $40 \%$ Bajaj and $60 \%$ TVS? (b) $40 \%$ TVS and 60\% Bajaj?

Illustration 15
Mr. X is interested to build a portfolio of investment comprising of risk-free securities $\left(\mathrm{R}_{\mathrm{f}}=\right.$ $8 \%$ ) and the market portfolio ( $\mathrm{R}_{\mathrm{m}}=18 \%$ and Standard deviation $=6 \%$ ). The minimum expected rate of return of the investor is $15 \%$. In what proportion should he hold the risk-free securities and the market portfolio? Also calculate the expected risk if correlation between the two stock is 0.24 .

## Illustration 16

(a) Stock A has an expected return of $18 \%$ and a standard deviation of $30 \%$. Stock B has expected return of $12 \%$ and a standard deviation of $36 \%$. The correlation between the two stocks is 0.25 if you form a portfolio where you put $40 \%$ of your money in A and $60 \%$ in B, what is the expected return and standard deviation for the portfolio?
(b) How will the excepted return and standard deviation change if the correlation between the two stocks is zero?

Illustration 17
You have decided to invest $40 \%$ of your wealth in McDonalds which has an excepted return of $15 \%$ and a standard deviation of $15 \%$, and $60 \%$ of your wealth in GE which has an excepted return of $9 \%$ and a standard deviation of $14 \%$.
a) What is the excepted return of your portfolio?
b) If the correlation between McDonalds and GM is 0.5 , what is the standard deviation of your portfolio?
c) If you wanted an excepted return of $13 \%$, what percentage should you invest in McDonalds?

Based on your percentage in part C , what would the standard deviation of this portfolio be?

## Illustration 18

Following are the price and other details of three stocks for the year 2011. Calculate the total return as well as the return relative for each of three stocks.

| Stock | Beginning Price | Dividend Paid | Ending Price |
| :--- | :--- | :--- | :--- |
| A | 30 | 3.40 | 34 |
| B | 72 | 4.70 | 69 |
| C | 140 | 4.80 | 146 |

Illustration 19
During the past five years, the returns of a stock were as follows:

| Year | Return |
| :--- | :--- |
| 1 | 0.07 |
| 2 | 0.03 |
| 3 | -0.09 |
| 4 | 0.06 |
| 5 | 0.10 |

Compute the following: (a) cumulative wealth index, (b) arithmetic mean, (c) geometric mean, (d) variance, and (e) standard deviation.

Illustration 20
You are thinking of acquiring some shares of ABC Ltd. The rates of return expectations are as follows:

| Possible rate of return | Probability |
| :--- | :--- |
| 0.05 | 0.20 |
| 0.10 | 0.40 |
| 0.08 | 0.10 |


| 0.11 | 0.30 |
| :--- | :--- |

Compute the expected return $\mathrm{E}(\mathrm{R})$ on the investment.
Illustration 21
The returns of two assets under four possible states of nature are given below:

| State of nature | Probability | Return on asset 1 | Return on asset 2 |
| :--- | :--- | :--- | :--- |
| 1 | 0.10 | $5 \%$ | $0 \%$ |
| 2 | 0.30 | $10 \%$ | $8 \%$ |
| 3 | 0.50 | $15 \%$ | $18 \%$ |
| 4 | 0.10 | $20 \%$ | $26 \%$ |

a. What is the standard deviation of the return on asset 1 and asset 2 ?
b. What is the covariance between the returns on assets 1 and 2?
c. What is the coefficient of correlation between the returns on assets 1 and 2 ?

Illustration 22
A portfolio consists of 3 securities, 1,2 , and 3 . The proportions of these securities are $w_{1}=$ $0.3, w_{2}=0.5$, and $w_{3}=0.2$. The standard deviations of returns on these securities (in percentage terms) are: $=6,=9$, and $=10$. The correlation coefficients among security returns are $p_{12}=$ $0.4, p_{13}=0.6, p_{23}=0.7$. What is the standard deviation of portfolio returns?

## Illustration 23

The following information is available.

|  | Stock A |  | Stock B |
| :--- | :--- | :--- | :--- |
| Expected return | $16 \%$ | 0.60 | $12 \%$ |
| Standard deviation | $15 \%$ |  | $8 \%$ |
| Coefficient of correlation |  |  |  |

(a) What is the covariance between stocks $A$ and $B$ ?
(b) What is the expected return and risk of a portfolio in which $A$ and $B$ have weights of 0.6 and 0.4 ?

## Illustration 24

The rate of return on stocks of Ben and Ten under different states of the economy are presented below along with the probability of the occurrence of each state of the economy.

| Particulars | Boom | Normal | Recession |
| :--- | :--- | :--- | :--- |
| Probability of occurrence | 0.3 | 0.5 | 0.2 |
| Rate of Return on Stock Ben (\%) | 25 | 35 | 45 |
| Rate of Return on Stock Ben (\%) | 45 | 35 | 25 |

(i) Calculate the expected rate of return and standard deviation of return on stock Ben and Ten.
(ii) If you could invest in either stock Ben or stock Ten, but not in both, which stock would you prefer?

Illustration 25
Ms. Manasi has invited in Mumbai and Goa Limited in the proportion of $40 \%$ and $60 \%$. The returns from these companies are given below:-

| Year | Mumbai Limited | Goa Limited |
| :--- | :--- | :--- |
| 1 | $20 \%$ | $24 \%$ |
| 2 | $30 \%$ | $36 \%$ |

Standard Deviation of both the companies is 3 .
Calculate:
(i) Expected return of Manasi's portfolio
(ii) Covariance between Mumbai Limited and Goa Limited.
(iii) Portfolio Risk for Manasi.

## Illustration 26

(A) Explain Capital Market Line with suitable diagram and example.
(B) Solve following:

| Particulars | Initial Price | Market Price <br> (at the end of the year) | Beta Risk factor |
| :--- | :--- | :--- | :--- |
| A | 13 | 19 | 1.25 |
| B | 20 | 25 | 1.00 |
| C | 24 | 30 | 1.33 |

Risk-free Return may be taken at $10 \%$ you are required to calculate.
(i) Expected Rate of Return of Portfolio in each by using CAPM
(ii) Average Returns of Portfolio

Illustration 27
The stock of Box Limited performs relatively well to other stocks during recessionary periods. The stock of Cox Limited, on the other hand, does well during growth periods. Both the stocks are currently selling for 100 per share. You assess the rupee return (dividend plus price) of these stocks for the next year as follows:

|  | Economic Condition |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | High growth | Low growth | Stagnation | Recession |
| Probability | 0.3 | 0.4 | 0.2 | 0.1 |
| Return on Box's stock | 100 | 110 | 120 | 140 |
| Return on Cox's stock | 150 | 130 | 90 | 60 |

Calculate the expected return and standard deviation of investing:
(a) 1,000 in the equity stock of Box Limited
(b) 1,000 in the equity stock of Cox Limited
(c) 500 each in the equity stock of Box Limited and Cox Limited.

Illustration 28
The Returns of 2 Assets, under four possible states of nature, are given below:-

| State of Nature | Probability | Returns on Asset 01 | Returns on Asset 02 |
| :--- | :--- | :--- | :--- |
| 1 | 0.10 | $5 \%$ | $0 \%$ |
| 2 | 0.30 | $10 \%$ | $8 \%$ |
| 3 | 0.50 | $15 \%$ | $18 \%$ |
| 4 | 0.10 | $20 \%$ | $26 \%$ |

Find out: (i) Standard Deviation for Asset 01 and Asset 02.
(ii) Co-variance between Returns of Asset 01 and 02.
(MU,BMS, Apr. 2011)
Illustration 29
Solve following:

| Particulars | Initial Priel | Market Priel <br> (at the end of the year) | Beta Risk facton |
| :--- | :--- | :--- | :--- |
| A | 13 | 19 | 1.25 |
| B | 20 | 25 | 1.00 |
| C | 24 | 30 | 1.33 |

Risk-free Return may be taken at $10 \%$ you are required to calculate.
(i) Expected Rate of Return of Portfolio in each by using CAPM.
(ii) Average Returns of Portfolio.

## Illustration 30

Mr. Anil purchased 2500 shares, of JKL Ltd. @ 20/- each (Face Value 5 per share) and paid brokerage @ $2 \%$ on 01-01-2009. The company paid dividend @ $50 \%$ each year he sold all the shares at 25/- each on 31-12-2010 and paid brokerage of 1,200/-.

The other investment alternative available to him was SBI Fixed Deposit carrying interest @ $12 \%$ p.a., for year on compounded basis.

Was his decision to go for share investment right? Offer your comments with reasoning.
(MU, BMS, Apr. 2011)

## Illustration 31

Mr. Anil purchased 200 Shares of JKL Ltd. @ 200/- each (Face Value 5 per share) and paid brokerage @ $1.50 \%$ on 01-01-2009. On 17-07-2010 the company declared Bonus Shares in the ratio of 1:1. He received no dividend on these shares in 2009. But on 24-12-2010 the company paid dividend @ $40 \%$ dividend. He sold all the shares at 150/- each on 31-12-2010 and paid brokerage of $1,200 /-$. What is the yearly rate of return on his investment?

Rate the quality of the investment as a Investment Consultant.
(MU, BMS, Oct. 2011)

